MASTERCLASS

# Understanding and interpreting confidence and credible intervals around effect estimates 

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#### Abstract

Introduction: Reporting confidence intervals in scientific articles is important and relevant for evidence-based practice. Clinicians should understand confidence intervals in order to determine if they can realistically expect results similar to those presented in research studies when they implement the scientific evidence in clinical practice. The aims of this masterclass are: (1) to discuss confidence intervals around effect estimates; (2) to understand confidence intervals estimation (frequentist and Bayesian approaches); and (3) to interpret such uncertainty measures. Content: Confidence intervals are measures of uncertainty around effect estimates. Interpretation of the frequentist $95 \%$ confidence interval: we can be $95 \%$ confident that the true (unknown) estimate would lie within the lower and upper limits of the interval, based on hypothesized repeats of the experiment. Many researchers and health professionals oversimplify the interpretation of the frequentist $95 \%$ confidence interval by dichotomizing it in statistically significant or non-statistically significant, hampering a proper discussion on the values, the width (precision) and the practical implications of such interval. Interpretation of the Bayesian $95 \%$ confidence interval (which is known as credible interval): there is a $95 \%$ probability that the true (unknown) estimate would lie within the interval, given the evidence provided by the observed data.


[^0]Conclusions: The use and reporting of confidence intervals should be encouraged in all scientific articles. Clinicians should consider using the interpretation, relevance and applicability of confidence intervals in real-world decision-making. Training and education may enhance knowledge and skills related to estimating, understanding and interpreting uncertainty measures, reducing the barriers for their use under either frequentist or Bayesian approaches.
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## Introduction

A paper published within this issue of the Brazilian Journal of Physical Therapy (BJPT) raised a very interesting, important and relevant matter for evidence-based practice: the use of the $95 \%$ confidence interval (CI) for reporting the uncertainty around between-group comparisons in randomized controlled trials investigating the effects of physical therapy interventions. ${ }^{1}$ Briefly, the study found that: (1) only less than one-third of physical therapy trials report Cls; (2) trials with lower risk of bias (i.e., higher quality) are more likely to report Cls; and (3) there has been a consistent increase in reporting Cls over time. ${ }^{1}$ The increasing trend on reporting Cls is good news for physical therapy evidencebased practice. Nevertheless, clinicians should understand Cls so they can appropriately interpret results of trials in order to better implement such evidence in practice. Therefore, this masterclass is aimed at: (1) discussing Cls around effect estimates on continuous (mean and mean difference) and dichotomous (proportion, odds, absolute risk reduction [ARR], relative risk [RR] and odds ratio [OR]) outcomes; (2) understanding Cls estimation (frequentist and Bayesian approaches); and (3) interpreting such uncertainty measures. We believe that this initiative might help clinicians to achieve the purpose of better understanding and interpreting uncertainty measures around effect estimates.

## What are confidence intervals?

ACl is a measure of the uncertainty around the effect estimate. It is an interval composed of a lower and an upper limit, which indicates that the true (unknown) effect may be somewhere within this interval. The effect presented in the scientific report must always be inside the Cl reported, and the width of the interval represents the precision of the effect estimate. Therefore, the narrower the Cl the more precise is the effect estimate. The Cl width (degree of uncertainty) varies according to two factors: (1) sample size ( $n$ ); and (2) heterogeneity (standard deviation [SD] or standard error [SE]) contained in the study. The sample size is inversely proportional to the degree of uncertainty; the larger the sample size, the smaller the CI width, which would indicate a lower degree of uncertainty. However, heterogeneity is directly proportional to the degree of uncertainty; the lower the heterogeneity the lower the uncertainty. This means that studies presenting lower SDs or SEs have a lower degree of uncertainty and a narrower Cl .

The confidence (probability) level (i.e., 95\%) of the Cl represents the accuracy of the effect estimate. ${ }^{2}$ For example, the $99 \% \mathrm{Cl}$ is more accurate than the $95 \% \mathrm{Cl}$, because it captures a broader spectrum of the data distribution. Thereby, the $99 \% \mathrm{Cl}$ is wider than the $95 \% \mathrm{Cl}$. However, the trade-off is that the $99 \% \mathrm{Cl}$ is less precise than the $95 \% \mathrm{Cl}$. The decision of using a certain confidence level should consider a balance between accuracy and precision. In health sciences the $95 \%$ confidence level is most often used. Two common approaches to estimate Cls are the frequentist and the Bayesian. In the next sections we will discuss the following topics related to both approaches: how to estimate; how to interpret; advantages; disadvantages; and illustrative examples (with case studies described in Boxes 1 and 2).

## Frequentist approach for Cls

The most known and widely used approach for statistical inference is the frequentist approach, also known as the classical (Neyman-Pearson) statistical approach. ${ }^{3,4}$ The frequentist approach for statistical inference is based on sampling distributions and the Central Limit Theorem (CLT). ${ }^{3,5}$ This explains the term "long-run frequency" attached to the interpretation of outcomes estimated using this approach (see the section "Interpreting frequentist 95\% CIs"), and the term "frequentist" to refer to this statistical thinking. The frequentist approach treats the population parameters of interest as fixed values. ${ }^{2,3,6}$

For example, let's assume a population distribution with mean $(\mu)=0$ and SD $(\sigma)=5$ (Fig. 1A). In reality, we usually do not know the true mean and standard deviation in the population; however, for the sake of examples, we are defining the population distribution in Fig. 1A. Let us say a researcher has collected data from this population, and the sample mean $\left(\bar{x}_{1}\right)=0.4$ and the sample SD $\left(s_{1}\right)=4.8$ (Fig. 1B, "Data collected''). The sample mean is considered the best guess of the sampling distribution mean (i.e., the mean of the sample means represented by Fig. 1C). In turn, the sampling distribution (Fig. 1C) is considered a long-run frequency of samples, including the one the researcher has collected data (sample 1 in Fig. 1B, "Data collected''), but also considering a set of hypothetical samples (samples 2-100 represented in Fig. 1B, "Hypothetical samples") that do not exist (i.e., the researcher has not collected data for this hypothetical samples). This has some implications that are discussed in the section "Disadvantages of frequentist 95\% CIs".

Box 1: Case study of a randomized controlled trial (RCT) with a continuous outcome.
Parreira et al. ${ }^{21}$ have conducted a RCT aimed at investigating the effects of Kinesio Taping applied according to the manuals ( $n_{1}=74$ ) compared to sham applications ( $n_{C}=74$ ) in individuals with chronic nonspecific low back pain. One of the primary outcomes was pain intensity measured with a numeric pain rating scale (NPRS) ranging from 0 (no pain) to 10 (worst possible pain). The table below describes the results for each group at baseline and after four weeks from baseline.

|  | Intervention group Mean (SD) | Comparison group Mean (SD) | Mean between-group diff (95\% CI) |
| :--- | :---: | :---: | ---: |
| Baseline | $7.0(2.0)$ | $6.8(2.0)$ | $0.2(-0.4$ to 0.8$)$ |
| 4 weeks | $4.4(2.8)$ | $4.6(2.5)$ | $-0.2(-1.1$ to 0.7$)$ |
| Within-group diff | $-2.6(3.1)$ | $-2.2(2.7)$ | $-0.4(-1.3$ to 0.5$)$ |

SD, standard deviation. CI, frequentist confidence interval. '"diff", difference.

## Mean difference between groups

The recommended outcome of RCTs investigating continuous variables, as the NPRS, is the between-group difference of the within-group difference. This outcome is usually obtained from the regression coefficient representing the interaction term composed of group and time in linear mixed models. ${ }^{22}$ Simplifying, the interaction term can also be estimated using a table like the one above. Therefore, the effect found for pain intensity after four weeks from baseline in this study was -0.4 , which means that the intervention group reduced 0.4 more points in the 11-point NPRS compared to the control group.

## 95\% confidence interval (CI)

- Standard error (SE): Eq. (2.1)
- $\mathrm{SE}_{\text {diff }}=\sqrt{ }\left(\left(\left(n_{1}-1\right) S D_{1}^{2}\right)+\left(\left(n_{C}-1\right) \mathrm{SD}_{\mathrm{C}}{ }^{2}\right) /\left(n_{1}+n_{\mathrm{C}}-2\right)\right) \times \sqrt{ }\left(\left(1 / n_{1}\right)+\left(1 / n_{\mathrm{C}}\right)\right)$
- $\mathrm{SE}_{\text {diff }}=\sqrt{ }\left(\left(\left((74-1) 3.1^{2}\right)+\left((74-1) 2.7^{2}\right)\right) /(74+74-2)\right) \times \sqrt{ }((1 / 74)+(1 / 74))=0.478$
- $t$ (probability $=0.95 ; \mathrm{df}=74+74-2)=1.976346 \approx 1.96$
$-95 \% \mathrm{Cl}=\left(\right.$ mean $_{I}-$ mean $\left._{\mathrm{C}}\right) \pm\left(t \times \mathrm{SE}_{\text {diff }}\right)=(-2.6-(-2.2)) \pm(1.96 \times 0.478)=-1.3$ to 0.5
The $95 \%$ frequentist Cl around the effect found for pain intensity after four weeks from baseline in the study of Parreira et al. ${ }^{21}$ was -1.3 to 0.5 in the 11 -point NPRS. This means that we can be $95 \%$ confident that individuals with chronic nonspecific low back pain would present, on average, a mean difference between -1.3 and 0.5 when comparing the intervention with the comparison group, based on hypothesized repeats of the experiment. Since the $95 \% \mathrm{Cl}$ contains the null effect (i.e., zero), which represents the null hypothesis (i.e., no difference between the groups), we cannot be $95 \%$ confident that the intervention group would present a reduced pain intensity compared to the comparison group in repeats of the experiment, as suggested by the effect estimate (i.e., -0.4 ). Therefore, we can conclude that this effect was not statically significant, which means that this evidence supports the null hypothesis. In other words, there was no difference between the groups.

There are several methods for estimating frequentist $95 \%$ Cls. In this masterclass we will describe the methods implemented in the Physiotherapy Evidence Database (PEDro) CI calculator, which can be downloaded in English at https://www.pedro.org.au/english/downloads/confidence -interval-calculator/. ${ }^{7}$ The reader can follow the estimations described in the case studies in Boxes 1 and 2 using the PEDro Cl calculator.

## Estimating frequentist Cls

## Mean

Eq. (1) describes Cl formula for a mean ( $\bar{x}$ ). The critical value " $t$ "' is based on the $t$ distribution attached with a particular probability level and degrees of freedom. For a $95 \% \mathrm{CI}$, the probability level must be set as 0.95 (or $95 \%$ ) and the degrees of freedom are determined by subtracting 1 from the sample size ( $n-1$ ). The SE of the sample mean can be estimated by Eq. (1.1).
$C I_{\bar{x}}=\bar{x} \pm\left(t \times S E_{\bar{x}}\right)$
$S E_{\bar{x}}=\frac{S D_{\bar{x}}}{\sqrt{n}}$

## Mean difference

Eq. (2) describes the Cl calculation for a mean difference $\left(\bar{x}_{1}-\bar{x}_{2}\right)$. The critical value " $t$ '' is based on the $t$ distribution attached with a particular probability level and degrees of freedom. For a $95 \% \mathrm{Cl}$, the probability level must be set as 0.95 (or $95 \%$ ) and the degrees of freedom are determined by subtracting 2 from the overall sample size $\left(n_{1}+n_{2}-2\right)$. " $S E_{\text {diff" }}$ refers to the SE of the difference between the two sample means assuming equal variances (Eq. (2.1)). Box 1 describes a case study using mean difference and its $95 \% \mathrm{Cl}$.

$$
\begin{equation*}
C l_{\text {diff }}=\left(\bar{x}_{1}-\bar{x}_{2}\right) \pm\left(t \times S E_{\text {diff }}\right) \tag{2}
\end{equation*}
$$

$$
S E_{\text {diff }}=\sqrt{\frac{\left(\left(n_{1}-1\right) \times S D_{1}^{2}\right)+\left(\left(n_{2}-1\right) \times S D_{2}^{2}\right)}{\left(n_{1}+n_{2}-2\right)}} \times \sqrt{\frac{1}{n_{1}}+\frac{1}{n_{2}}}(2.1)
$$

## Box 2: Case study of a randomized controlled trial (RCT) with a dichotomous outcome.

Mateus-Vasconcelos et al. ${ }^{23}$ have conducted a RCT aimed at investigating the effects of vaginal palpation, vaginal palpation associated with posterior pelvic tilt, and intravaginal electrical stimulation in facilitating voluntary contraction of the pelvic floor muscles in women with pelvic floor dysfunctions. This case study is considering only the vaginal palpation associated with posterior pelvic tilt as the intervention group ( $n_{1}=33$ ), and verbal instructions to perform pelvic floor muscle exercises at home as the comparison group ( $n_{c}=33$ ). The primary outcomes was the number of women who had changed in the Modified Oxford Scale (MOS) for pelvic floor muscle strength, ranging from 0 (no contraction) to 5 (strong contraction with lift). The table below describes, using a 2 by 2 table, the number of participants in each group who changed (improved) their pelvic floor muscle strength from MOS 0 or 1 to $\geq 2$ after eight weeks from baseline.

|  | Change | No change | Total |
| :--- | :--- | :--- | :--- |
| Intervention group | $\mathbf{A}=23$ | $\mathbf{C}=10$ | $A+C=33$ |
| Comparison group | $\mathbf{B}=6$ | $\mathbf{D}=27$ | $B+D=33$ |
| Total | $A+B=29$ | $C+D=37$ | $A+B+C+D=66$ |

## Relative risk ( $R R$ ) to compare groups

- Risk of intervention group $=A /(A+C)=0.697$ or $69.7 \%$
- Risk of comparison group $=B /(B+D)=0.182$ or $18.2 \%$
- $\mathrm{RR}=(A /(A+C)) /(B /(B+D))=0.697 / 0.182=3.83$
- Standard error for RR (SE $\left.\mathrm{En}_{\mathrm{lRR})}\right)$ : Eq. (5.2)
- $\mathrm{SE}_{\operatorname{ln(RR)}}=\sqrt{ }((1 / A)-(1 /(A+C))+(1 / B)-(1 /(B+D)))=\sqrt{ }((1 / 23)-(1 /(33))+(1 / 6)-(1 /(33)))=0.387$
$-95 \% \mathrm{Cl}_{R R}=\mathrm{e}^{\ln (R R) \pm(Z \times S E \ln (R R))}=\mathrm{e}^{1.342865 \pm(1.96 \times 0.387)}=\mathrm{e}^{0.584345 \text { to } 2.101385}=1.79$ to 8.17


## 95\% confidence interval (CI) for RR

The $95 \%$ frequentist Cl around the RR found for pelvic floor muscle strength after eight weeks from baseline was 1.79 to 8.17 in the 6 -point MOS. This means that we can be $95 \%$ confident that women with pelvic floor dysfunctions would present, on average, an RR between 1.79 and 8.17 when comparing the intervention with the comparison group, based on hypothesized repeats of the experiment. Since the $95 \% \mathrm{Cl}$ does not contain the null effect (i.e., one), which represents the null hypothesis (i.e., the same risk for both groups), we can conclude that this effect was statically significant, which means that we can be $95 \%$ confident that the intervention would be effective on increasing the risk of women changing the MOS for the better, which means strengthen the pelvic floor muscles, compared to the comparison group in repeats of the experiment.

Odds ratio (OR) to compare groups

- Odds of intervention group $=(A /(A+C)) /(C /(A+C))=A / C=2.30$
- Odds of comparison group $=(B /(B+D)) /(D /(B+D))=B / D=0.2222 \ldots$
- $\mathrm{OR}=(A / C) /(B / D)=2.30 / 0.22=10.35$
- $\mathrm{SE}_{\ln (0 R)}$ : Eq. (6.2)
- $\mathrm{SE}_{\ln (O R)}=\sqrt{ }((1 / A)+(1 / B)+(1 / C)+(1 / D))=\sqrt{ }((1 / 23)+(1 / 6)+(1 / 10)+(1 / 27))=0.589$
$-95 \% \mathrm{Cl}_{\mathrm{OR}}=\mathrm{e}^{\ln (O R) \pm(z \times \operatorname{SE} \ln (O R))}=\mathrm{e}^{2.336987 \pm(1.96 \times 0.589)}=\mathrm{e}^{1.182547 \text { to } 3.491427}=3.26$ to 32.84
95\% confidence interval (CI) for OR

The $95 \%$ frequentist Cl around the OR found for pelvic floor muscle strength after eight weeks from baseline was 3.26 to 32.84 in the 6 -point MOS. This means that we can be $95 \%$ confident that women with pelvic floor dysfunctions would present, on average, an OR between 3.26 and 32.84 when comparing the intervention with the comparison group, based on hypothesized repeats of the experiment. Since the $95 \% \mathrm{Cl}$ does not contain the null effect (i.e., one), which represents the null hypothesis (i.e., the same odds for both groups), we can conclude that this effect was statically significant, which means that we can be $95 \%$ confident that the intervention would be effective on increasing the odds of women changing the MOS for the better, which means strengthen the pelvic floor muscles, compared to the comparison group in repeats of the experiment.

## Proportion and odds

Eq. (3) describes the Wilson score method ${ }^{8,9}$ to estimate the Cl for a proportion (p). The critical value " $z$ '" is based on the normal (Gaussian) distribution attached with a particular probability level. For a $95 \% \mathrm{Cl}$, the critical value ' $z$ ' ' is
approximately 1.96 . The odds and its $95 \% \mathrm{Cl}$ can be obtained by converting the proportions to odds using Eq. (3.1).

$$
\begin{equation*}
C I_{p}=\frac{2 n p+z^{2} \pm z \sqrt{\left(z^{2}+4 n p(1-p)\right)}}{2\left(n+z^{2}\right)} \tag{3}
\end{equation*}
$$



Figure 1 Graphical representation of: (A) a population distribution; (B) samples 1 to 100 from the population distribution ( $n=100$ for each sample); and ( $C$ ) the sampling distribution. " $N$ ", population size. " $n$ ", sample size. " $\mu$ ", population mean. " $\sigma$ ", population standard deviation. " $\bar{x}$ ", sample mean. " $s$ ", sample standard deviation. "SE", standard error. "Cl', confidence interval.
odds $=\frac{p}{1-p}$

## Absolute risk reduction (ARR)

Eqs. (4.1) and (4.2) describe the Newcombe-Wilson method ${ }^{9,10}$ to estimate the lower $\left(L C I_{A R R}\right)$ and upper $\left(U C I_{A R R}\right)$ limits of the CI for the ARR, respectively. The letters " $L$ " and " $U$ "' represents the lower and upper limits of the proportions for groups 1 and 2, which can be estimated using Equation 3.
$L C I_{A R R}=\left(p_{1}-p_{2}\right)-z \sqrt{\frac{U_{2}\left(1-U_{2}\right)}{n_{2}}+\frac{L_{1}\left(1-L_{1}\right)}{n_{1}}}$
$U C I_{A R R}=\left(p_{1}-p_{2}\right)+z \sqrt{\frac{U_{1}\left(1-U_{1}\right)}{n_{1}}+\frac{L_{2}\left(1-L_{2}\right)}{n_{2}}}$

## Relative risk (RR) and odds ratio (OR)

Eqs. (5) and (6) describe the Cl calculation for the RR and for the OR, respectively. ${ }^{11}$ In Eqs. (5.1), (5.2), (6.1) and (6.2), " $A$ ", represents the number of individuals with the event in group 1; " $B$ '" represents the number of individuals with the event in group 2; " $C$ " represents the number of individuals without the event in group 1; and " $D$ " represents the number of individuals without the event in group 2. These values
can be determined in a 2 by 2 table. ${ }^{11}$ Box 2 describes a case study using RR, OR and their respective $95 \%$ Cls.
$C I_{R R}=e^{\ln (R R) \pm\left(z \times S E_{\ln (R R)}\right)}$
$R R=\frac{a /(a+c)}{b /(b+d)}$
$S E_{\ln (R R)}=\sqrt{\frac{1}{a}-\frac{1}{a+c}+\frac{1}{b}-\frac{1}{b+d}}$
$C l_{O R}=\mathrm{e}^{\ln (O R) \pm\left(z \times S E_{\ln (O R)}\right)}$
$O R=\frac{a d}{b c}$
$S E_{\ln (O R)}=\sqrt{\frac{1}{a}+\frac{1}{b}+\frac{1}{c}+\frac{1}{d}}$

## Interpreting frequentist Cls

The frequentist Cl has a long-run frequency interpretation, that is: random samples from the same target population and with the same sample size would yield Cls that contain the true (unknown) estimate in a frequency (percentage) set by the confidence level. However, we usually do not have several random samples from the same population; instead we collect data from only one sample of the population of interest and compute the Cl for this particular sample. The interpretation of this particular Cl would be: we can be XX\% confident that the true (unknown) estimate would lie within the lower and upper limits of the CI , based on hypothesized repeats of the experiment.

For the $95 \% \mathrm{Cl}$, this would imply that if we repeat an experiment 100 times and compute the $95 \% \mathrm{Cl}$ for all 100 experiments (Fig. 1B), then 95 ( $95 \%$ ) of these Cls would contain the true (unknown) estimate, while 5 (5\%) of these Cls would not contain the true (unknown) estimate. This true (unknown) estimate is represented in Fig. 1C by the mean of the sampling distribution (i.e., "mean of $\bar{x}_{1: 100}=0.0$ ''), which frequentists use as a proxy for the population mean represented by Fig. 1A. But let us suppose we have collected data from only one sample of the target population (which is usually the case), that is represented by the sample "Data collected'" in Fig. 1B. The $95 \% \mathrm{Cl}$ yielded from this particular sample can be interpret as follows: we can be $95 \%$ confident that the true (unknown) estimate would lie within the lower and upper limits of the Cl , based on hypothesized repeats of the experiment.

Regarding statistical significance, if the Cl does not contain the null hypothesized value, this would indicate statistical significance for the particular significance level set by the investigator. For example, in case of a between-group mean difference in a randomized controlled trial, the null hypothesized value represented by the null hypothesis $\left(H_{0}\right)$ is zero (i.e., no difference between the groups: $\bar{x}_{1}-\bar{x}_{2}=0$ ). If the $95 \% \mathrm{Cl}$ does not contain zero and the limits are negative (e.g., -4.0 to -1.0 ; Fig. 2A) this means that we can be $95 \%$ confident that the true (unknown) between-group mean difference would, on average, lie within negative values, indicating that we can be $95 \%$ confident that the intervention group would present a lower mean compared to the comparison group. Moreover, if the $95 \% \mathrm{Cl}$ does not contain
zero and the limits are positive (e.g., 0.5 to 3.5 ; Fig. 2C) this means that we can be $95 \%$ confident that the true (unknown) between-group mean difference would, on average, lie within positive values, indicating that we can be $95 \%$ confident that the intervention group would present a higher mean compared to the comparison group. Both scenarios would indicate a statistically significant result at a significance level of $0.05(1-0.95)$ or $5 \%$, since both Cls do not contain zero. These results would certainly yield a $p$-value lower than 0.05 . However, if the $95 \% \mathrm{Cl}$ contains zero (e.g., -2.0 to 1.0 ; Fig. 2B) this means that we can be $95 \%$ confident that the true (unknown) between-group mean difference would, on average, lie within a negative and a positive value, indicating that we cannot be $95 \%$ confident that the intervention group would present a lower or a higher mean compared to the comparison group. This would indicate a non-statistically significant result, certainly yielding a $p$-value higher than 0.05 (for another example and interpretation, see Box 1).

In case of ratios, such as RR and OR, the null hypothesized value represented by the null hypothesis $\left(H_{0}\right)$ is 1 (i.e., same proportion or odds in both groups: $p_{1} / p_{2}=1$ ). If the $95 \% \mathrm{Cl}$ does not contain 1 and the limits are lower than 1 (e.g., 0.40 to 0.80 ; Fig. 2D) this means that we can be $95 \%$ confident that the true (unknown) ratio would, on average, lie within values lower than 1, indicating that we can be 95\% confident that the intervention group would present a lower event proportion compared to the comparison group. Moreover, if the $95 \% \mathrm{Cl}$ does not contain 1 and the limits are higher than 1 (e.g., 2.0 to 3.0; Fig. 2F) this means that we can be $95 \%$ confident that the true (unknown) ratio would, on average, lie within values higher than 1 , indicating that we can be $95 \%$ confident that the intervention group would present a higher event proportion compared to the comparison group. Both scenarios would indicate a statistically significant result at a significance level of $0.05(1-0.95)$ or $5 \%$, since both Cls do not contain 1 . These results would certainly yield a $p$-value lower than 0.05 . However, if the $95 \%$ Cl contains 1 (e.g., 0.70 to 1.50 ; Fig. 2E) this means that we can be $95 \%$ confident that the true (unknown) ratio would, on average, lie within a value lower than 1 and a value higher than 1 , indicating that we cannot be $95 \%$ confident that the intervention group would present a lower or a higher event proportion compared to the comparison group. This would indicate a non-statistically significant result, certainly yielding a $p$-value higher than 0.05 (for another example and interpretation, see Box 2). The same interpretation approach for RR can also be applied to OR. However, one should note that RR and OR are not the same measure (Box 2).

## Advantages of using frequentist Cls rather than $p$-values

The frequentist approach is well known for performing hypothesis testing. Frequentist hypothesis testing lies in accepting or rejecting the null hypothesis $\left(H_{0}\right)$ by calculating the famous " $p$-value". The $p$-value is defined as the probability of observing the acquired or a more extreme result in a hypothetical series of repeats of the experiment (i.e., sampling distribution), given that the null hypothesis


Figure 2 Graphical representation of statistically significant ( $A, C, D$, and $F$ ) and non-statistically significant ( $B$ and $E$ ) results for frequentist $95 \%$ confidence intervals or Bayesian $95 \%$ credible intervals. For simplicity, both frequentist and Bayesian intervals are interchangeable in this figure, and they are represented with the acronym "Cl'. "RR", relative risk. "OR'", odds ratio.
is true. ${ }^{3,4}$ Health science researchers usually define a significance level of 0.05 (or $5 \%$ ) for hypothesis testing. Therefore, one rejects the null hypothesis when a $p$-value is smaller than 0.05 , which means that the probability of observing the actual or a more extreme estimate, given that the null hypothesis is true, is very low, supporting the conclusion that the null hypothesis might not be true. On the other hand, one accepts the null hypothesis when a $p$-value is equal to or greater than 0.05, which means that the probability of observing the actual or a more extreme estimate, given that the null hypothesis is true, is moderate to high, supporting the conclusion that the null hypothesis might be actually true. Another simple way of interpreting $p$-values is the following: the smaller the $p$-value the greater the evidence against the null hypothesis and, therefore, the results suggest that the alternative hypothesis $\left(H_{1}\right)$ might be more likely.

However, criticisms have been raised on how researchers and health professionals have been misinterpreting, misusing, and overemphasizing frequentist hypothesis testing,
especially the $p$-value. ${ }^{4,12,13}$ These criticisms include the following ${ }^{3,4,12-14}$ :

- The $p$-value is not the probability that the null hypothesis is (or is not) true, which would be formally represented as $p\left(H_{0} \mid y\right)$; " $H_{0}$ "' represents the null hypothesis and " $y$ '" represents the observed data. However, many researchers and health professionals are tempted to interpret the $p$ value this way, leading to misinterpretations. Actually, the $p$-value is a measure of the extremeness of the actual result given the null hypothesis, which may be formally represented as $p\left(y \mid H_{0}\right)$. Perhaps due to non-familiarity with these concepts, the $p$-value interpretation most used in research and in practice is dichotomized, i.e., statistically significant or not statistically significant based on a threshold of 0.05 . This may avoid the probability misinterpretation of $p$-values, but also oversimplifies the information provided by them.
- The dichotomized interpretation approach of $p$-values, which are widely used in research and in practice, allows
for accepting or rejecting the null hypothesis without questioning the effect size or the variability (e.g., uncertainty or precision) of the effect estimate.
- The $p$-value seems to have a large sample-to-sample variability, indicating that this measure is probably not reliable on indicating the strength of evidence against the null hypothesis.

The frequentist Cl has been suggested as an alternative to $p$-values. ${ }^{12,13}$ It has the advantage of describing the variability of the estimate and its width indicates the precision of the estimate. ${ }^{2}$ Therefore, researchers have recommended that effect estimates should be followed by their Cls (usually with a $95 \%$ confidence level) in scientific reportings. ${ }^{1,15}$ However, the current use of the frequentist CI has also raised some concerns, which would be discussed in the next section (i.e., "Disadvantages of using frequentist Cls'’).

## Disadvantages of using frequentist Cls

We believe that the use of the frequentist Cl has two potential disadvantages. Firstly, the long-run frequency interpretation of the frequentist Cl is not friendly. Therefore, many researchers and health professionals have misinterpreted the frequentist $\mathrm{Cl} .{ }^{15}$ For the $95 \% \mathrm{Cl}$, a common misinterpretation is the following: there is a $95 \%$ probability that the true (unknown) effect estimate lies within the $95 \% \mathrm{Cl}$. This interpretation is not accurate for the frequentist Cl , since the frequentist approach treats the population parameter as a fixed (unknown) value and, therefore, this fixed value is either inside or outside the interval with $100 \%$ (or $0 \%$ ) probability. ${ }^{2,6}$ Actually, the "probability interpretation" that clinicians usually use in clinical practice refers to the Bayesian interval (see the section "Bayesian approach for CIs"). ${ }^{3,15}$ Thereby, the accurate interpretation for the frequentist $95 \% \mathrm{Cl}$ would be the following: if we repeat an experiment over and over again (graphically represented by Fig. 1B) and we compute the $95 \% \mathrm{Cl}$ for all experiments, then $95 \%$ of these Cls would contain the true (unknown) estimate (represented by "mean of $\bar{x}_{1: 100}$ "' in Fig. 1C), while $5 \%$ of these Cls would not contain the true (unknown) estimate (Boxes 1 and 2). A graphical representation of the frequentist $95 \% \mathrm{Cl}$ can be found in Fig. 1B

Secondly, many researchers and health professionals oversimplify the interpretation of the frequentist $95 \%$ Cl by dichotomizing it in statistically significant or nonstatistically significant and, therefore, hampering a proper discussion on the values, the width (i.e., precision) and the practical implications of such interval. This would lead to some limitations and criticisms discussed earlier in this masterclass for the use of $p$-values, ruling out the advantages of using frequentist Cls rather than $p$-values. Therefore, there is no additional benefit in replacing the use of $p$-values by an oversimplified (i.e., dichotomized) interpretation of the frequentist Cl .

## Illustrative example of frequentist Cls

A randomized controlled trial had investigated the effectiveness of back school versus McKenzie exercises in individuals
with chronic nonspecific low back pain. ${ }^{16}$ The primary outcomes were pain intensity ( $0-10$ pain numerical rating scale) and disability (Roland-Morris Disability Questionnaire analyzed as a 0-24 numeric scale) one month after randomization. The between-group difference (adjusted for within-group differences) for pain intensity was 0.66 with a $95 \% \mathrm{Cl}$ of -0.29 to 1.62 , meaning that we can be $95 \%$ confident that the true (unknown) effect would lie between -0.29 and 1.62 , based on hypothesized repeats of the experiment. For disability, the between-group difference (adjusted for within-group differences) was 2.37 in favor of McKenzie with a $95 \% \mathrm{Cl}$ of 0.76 to 3.99 , meaning that we can be $95 \%$ confident that the true (unknown) effect would lie between this CI , based on hypothesized repeats of the experiment. The null hypothesized effect was zero (i.e., no difference between groups). The $95 \% \mathrm{Cl}$ for pain intensity contained the null effect (i.e., zero), meaning that the result was not statistically significant. For disability, the 95\% CI did not contain the null effect, meaning that the result was statistically significant. Up to now, the conclusions would be the same if one had used the dichotomized interpretation of $p$-values instead of the dichotomized interpretation of Cls. However, despite significance, the effect for disability was considered small, because in this case, clinicians could expect that their clinical results for disability would fall approximately within 0.76 to 3.99 points on a 0-24 points measure. This interpretation would not be possible when considering only the $p$-value (which only measures the extremeness of the result under the null hypothesis) or the dichotomized interpretation of the Cl . Therefore, the authors concluded that McKenzie exercise were not superior than back school for improving pain intensity in individuals with chronic nonspecific low back pain, and were only slightly more effective for disability. ${ }^{16}$

## Bayesian approach for Cls

Bayesian inference is a statistical approach aiming at estimating a certain parameter (e.g., a mean or a proportion) from the population distribution, given the evidence provided by the observed (i.e., collected) data. ${ }^{3}$ Therefore, the Bayesian approach for statistical inference is considered a more direct or natural approach to answer a research question, since it estimates the parameter of interest directly from the population distribution (Fig. 1A) instead of estimating from the sampling distribution as the frequentist approach (Fig. 1C). The Bayesian approach treats the parameters of interest as random variables, and, therefore, parameters can be described with probability distributions. ${ }^{3,17}$ One of the main characteristic of the Bayesian approach is the compromise of prior evidence with the observed data. Prior evidence and the observed data are represented with probability distributions that, in Bayesian terminology, are defined as prior and likelihood distributions, respectively. The prior distribution is combined with the likelihood distribution in order to update the previous knowledge, resulting in the posterior distribution, which is formally represented as $p(\theta \mid y)$; " $\theta$ " represents the parameter of interest and " $y$ "' represents the observed data. ${ }^{3}$

The outcome of a Bayesian analysis is the posterior distribution. The posterior distribution can be summarized by

Symmetric distribution


Figure 3 Graphical representation of symmetric ( $A$ and $B$ ), right (positive) skewed ( $C$ and $D$ ) and left (negative) skewed ( $E$ and F) distributions.
measures of central tendency (e.g., median, mean or mode) and measures of uncertainty (e.g., variance or standard deviation). One of the most used measures of uncertainty in Bayesian inference is the Bayesian credible interval (CrI), which is analogous to the Cl in the frequentist approach.

## Estimating Bayesian Crls

Describing and discussing the computation of posterior distributions are beyond the scope of this masterclass. However, once the posterior distribution that represents the updated knowledge about a parameter of interest is defined, obtaining the Crl is straightforward. There are typically two types of Bayesian Crls: (1) equal tail interval; and (2) highest posterior density (HPD) interval. The following sections
will be focused on defining, explaining and interpreting such intervals.

## Equal tail Crl

The Bayesian equal tail Crl method returns threshold values of the posterior distribution that represent an interval with the probability of interest (e.g., 95\%) of the distribution mass around the center of the distribution (Fig. 3A). In other words, the lower limit of the $95 \%$ equal tail Crl is the quantile representing a probability of 0.025 (or the $2.5 \%$ percentile) of the posterior distribution, while the upper limit of the equal tail CrI is the quantile representing a probability 0.975 (or the $97.5 \%$ percentile) of the posterior distribution. An advantage of estimating the equal tail Bayesian Crl is that this interval is easily calculated. However, a common
concern related to the equal tail Bayesian Crl is that it might yield estimate values with lower probability inside the interval than outside the interval when the posterior distribution is not symmetric (i.e., right or left skewed). ${ }^{3}$ When this occurs, the meaning would be that some values would have a higher probability of representing the parameter when outside the interval compared to some values inside the interval. Graphically, this would yield a shift line connecting the lower and upper limits for this interval (Fig. 3C and E). Since this situation is not desired, another method has been proposed in order to estimate Bayesian Crls: the HPD interval, which is discussed in the next section (i.e., "Highest posterior density (HPD) Crl'’).

## Highest posterior density (HPD) CrI

The Bayesian HPD Crl method returns threshold values of the posterior distribution that represent an interval with the probability of interest (e.g., 95\%) of the distribution mass around the center of the distribution, holding true the assumption that all values inside the interval have higher probabilities of representing the parameter than all the values outside the interval. For example, for a 95\% HPD Crl, the interval contains $95 \%$ of the mass of the posterior distribution around the center of the distribution, and all values inside the interval are more likely to represent the parameter than the values outside the interval. Graphically, this would always yield a straight line connecting the lower and upper limits for this interval (Fig. 3B, D and F). For symmetric posterior distributions, the HPD Crl is equivalent to the equal tail Bayesian Cl (Fig. 3A and B). ${ }^{3}$ A disadvantage of the HPD Crl method is that the computation of the interval is more complex compared to the equal tail Crl method, since the HPD Crl estimation requires numerical optimization. ${ }^{3}$

## Interpreting Bayesian Crls

Bayesian Crls have a more natural interpretation than frequentist Cls. ${ }^{3}$ This is due to the fact that the Bayesian CrI estimates the most likely values of the parameter of interest directly from the computed posterior distribution, which, in turn, represents all knowledge and evidence about the population distribution at the moment. The interpretation of the Bayesian $95 \% \mathrm{Crl}$ is the following: there is a $95 \%$ probability that the true (unknown) effect estimate (represented by " $\mu$ " in Fig. 1A) would lie within the interval, given the evidence provided by the observed data. ${ }^{3,15}$

The way we judge if there is a statistical significance result when interpreting the Bayesian Crl is similar to the frequentist Cl . However, one should note that the interpretation of the Bayesian Crl is rather different from the frequentist Cl . For example, in case of a between-group mean difference, the null effect is zero (i.e., no difference between the groups: $\bar{x}_{1}-\bar{x}_{2}=0$ ). Let us suppose that a $95 \% \mathrm{Crl}$ is composed of the following limits: -4.0 to -1.0 (Fig. 2A). This would indicate that there is a $95 \%$ probability that the population mean difference would lie between -4.0 and -1.0 , given the observed data. In other words, the most plausible values (i.e., -4.0 to -1.0 ) with higher probability of representing the true (unknown) estimate indicate that the mean of the intervention group would be lower compared to the comparison group, with at least a $95 \%$
probability. Moreover, let us suppose that a $95 \% \mathrm{Crl}$ is composed of the following limits: 0.5 to 3.5 (Fig. 2C). This would indicate that there is a $95 \%$ probability that the population mean difference would lie between 0.5 and 3.5 , given the observed data. In other words, the most plausible values (i.e., 0.5 to 3.5 ) with higher probability of representing the true (unknown) estimate indicate that the mean of the intervention group would be higher compared to the comparison group, with at least a $95 \%$ probability. Both scenarios would indicate a statistically significant result at a significance level of $0.05(1-0.95)$ or $5 \%$, since both Crls do not contain zero. However, in case of a $95 \% \mathrm{Crl}$ composed of the following limits: -2.0 to 1.0 (Fig. 2B), this would indicate that there is a $95 \%$ probability that the population mean difference would lie between -2.0 and 1.0 , given the observed data. Since the most plausible values (i.e., -2.0 to 1.0 ) with higher probability of representing the true (unknown) estimate indicate that the mean of the intervention group could be either lower or higher compared to the comparison group, this would indicate a non-statistically significant result.

In case of ratios, such as RR and OR, the null effect is 1 (i.e., same proportion or odds in both groups: $p_{1} / p_{2}=1$ ). Let us suppose that a $95 \% \mathrm{Crl}$ for an RR is composed of the following limits: 0.40 to 0.80 (Fig. 2D). This would indicate that there is a $95 \%$ probability that the population RR would lie between 0.40 and 0.80 , given the observed data. In other words, the most plausible values (i.e., 0.40 to 0.80 ) with higher probability of representing the true (unknown) estimate indicate that the event proportion of the intervention group would be lower compared to the comparison group, with at least a $95 \%$ probability. Moreover, let us suppose that a $95 \%$ Crl for an RR is composed of the following limits: 2.0 to 3.0 (Fig. 2F). This would indicate that there is a $95 \%$ probability that the population RR would lie between 2.0 and 3.0 , given the observed data. In other words, the most plausible values (i.e., 2.0 to 3.0 ) with higher probability of representing the true (unknown) estimate indicate that the event proportion of the intervention group would be higher compared to the comparison group, with at least a $95 \%$ probability. Both scenarios would indicate a statistically significant result at a significance level of $0.05(1-0.95)$ or $5 \%$, since both Crls do not contain 1. However, in case of a $95 \% \mathrm{Crl}$ composed of the following limits: 0.70 to 1.50 (Fig. 2E), this would indicate that there is a $95 \%$ probability that the population RR would lie between 0.70 and 1.50 , given the observed data. Since the most plausible values (i.e., 0.70 to 1.50 ) with higher probability of representing the true (unknown) estimate indicate that the event proportion of the intervention group could be either lower or higher compared to the comparison group, this would indicate a non-statistically significant result. The same interpretation approach of RR can also be applied to OR. However, one should note that RR and OR are not the same measure (Box 2).

## Advantages of using Bayesian Crls

A clear advantage of Bayesian Crls is the interpretability of such measures. For example, let us consider the frequentist $95 \% \mathrm{Cl}$ related to the effectiveness of back school compared to McKenzie exercises on disability discussed earlier in this
masterclass (see the section "Illustrative example of frequentist CIs''), that is 0.76 to 3.99 . As discussed earlier, the interpretation of this frequentist $95 \% \mathrm{Cl}$ is that, considering a hypothetical series of repeats of the experiment, we can be $95 \%$ confident that the true (unknown) effect estimate (represented by "mean of $\bar{x}_{1: 100}$ "' in Fig. 1C) would lie between 0.76 and 3.99. Now, let us suppose that this interval was estimated using Bayesian inference. Considering the same interval as a Bayesian CrI, the interpretation would be that there is a $95 \%$ probability that the true (unknown) effect estimate (represented by " $\mu$ "' in Fig. 1A) lies within 0.76 to 3.99 , given the observed data. The Bayesian CrI is considered to be easier to interpret than the frequentist CI , because:

- The Bayesian CrI can be interpreted in a probabilistic way, which clinicians usually use in clinical practice even for frequentist Cls. ${ }^{3}$ This indicates the preference of clinicians for this probabilistic interpretation.
- The Bayesian approach reflects a direct estimate from the population distribution (Fig. 1A) represented by the actual computed posterior distribution, instead of estimating from the hypothetical sampling distribution (Fig. 1B and C) in the frequentist approach.


## Disadvantages of using Bayesian Crls

A clear disadvantage of using Bayesian Crls is the complexity of computing posterior distributions, especially in complex problems/analyses conducted in, for example, randomized controlled trials. In the past, this imposed a very important barrier to the use of Bayesian inference. However, considering the recent advantages in computer science and technology, the use of Bayesian inference was significantly facilitated especially in complex situations. Therefore, computation issues should not preclude Bayesian analyses nowadays. However, knowledge and skills for performing such analyses are clearly remaining barriers that should be considered in biostatistics education for health scientists and for health professionals. This might generate work opportunities for clinicians, including physical therapists, as suggested by Casals and Finch. ${ }^{18,19}$

## Illustrative example of Bayesian Crls

A 6-month randomized controlled trial had investigated the effectiveness of an online tailored advice package (i.e., TrailS6) compared to general advice on preventing runningrelated injuries (RRI) in trail runners. ${ }^{20}$ The main result was presented by an ARR of $-13.1 \%$ (i.e., the intervention reduced the risk of sustaining RRIs in $13.1 \%$ ), with a $95 \%$ HPD CrI of $-23.3 \%$ to $-3.1 \%$. The interpretation of this $95 \%$ HPD CrI is that there was a $95 \%$ probability that the true (unknown) preventive effect would have been within -23.3\% to $-3.1 \% .^{20}$ In other words, the most plausible values (i.e., $-23.3 \%$ to $-3.1 \%$ ) with higher probability of representing the true (unknown) estimate indicate that the intervention group would present a lower risk of RRIs compared to the comparison group, with at least a $95 \%$ probability. We believe that this interval is more natural an easy-tointerpret than the frequentist CI . The authors of the trial
concluded that the online tailored advice package (TrailS6) was effective on preventing RRIs in trail runners.

## Conclusions

We believe that, as recommended by Freire et al., ${ }^{1}$ the use and reporting of $95 \% \mathrm{Cl}$ should be encouraged even when $p$-values are presented. Decision-making should neither be made considering only the dichotomized interpretation of $p$-values nor the dichotomized interpretation of Cls (i.e., statistically significant or non-statistically significant). Instead, a more in-depth analysis and interpretation of the values and width (i.e., precision) of Cls are recommended in order to avoid oversimplification of these rich measures. Frequentist Cls are alternative and preferable measures compared to $p$-values. However, the interpretability of the frequentist approach, which is based on hypothetical series of repeats of the experiment (i.e., sampling distribution) given that the null hypothesis is true, opens the opportunity for the use of Bayesian Crls, that are more naturally and easily interpretable. Training and education may enhance knowledge and skills related to estimating, understanding and interpreting uncertainty measures, reducing the barriers for their use under either frequentist or Bayesian approaches.

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## Conflicts of interest

The authors declare no conflicts of interest.

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